

# Deeply Virtual Compton Scattering in the Saturation Approach

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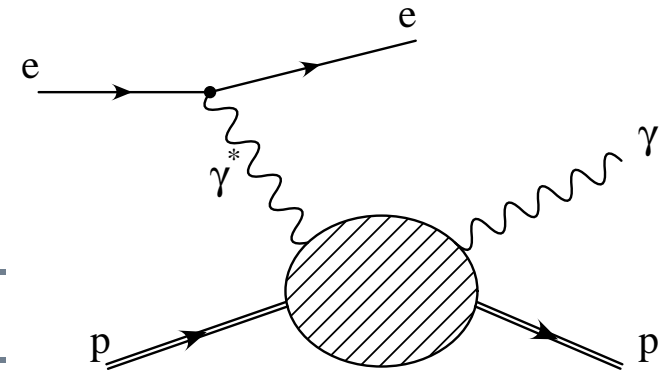
\*\* I.I.H.E., Université Libre de Bruxelles.

<http://www.h1-desy.de/~favart/dvcs>

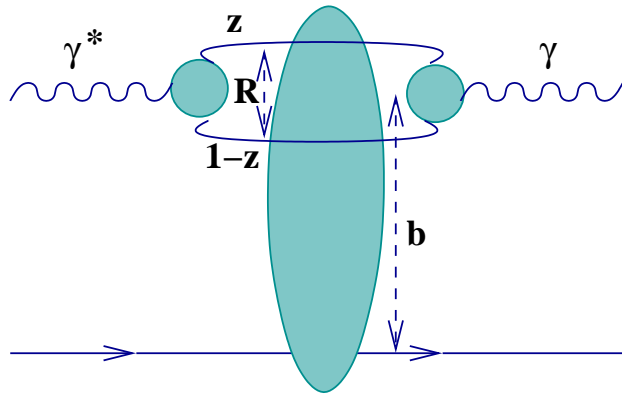
<http://www.if.ufrgs.br/~magnus/>

# Motivation

- DVCS is a very clear QCD process, having a real photon in the final state.
- DVCS can give access to real and imaginary parts of the QCD scattering amplitude through the interference with QED Bethe-Heitler (BH).
- At HERA, H1 and ZEUS measured DVCS in perturbative virtualities  $Q^2$ , and high energy.
- Saturation models can be easily extended to DVCS process.



# DVCS in Color Dipole



L.Favart-M.V.Machado,

Eur. Phys. J. C 29 (2003) 365-371.

$$\text{Im } \mathcal{A} = \int_0^1 dz \int d^2 \mathbf{r} \Phi_T(z, \mathbf{r}, Q^2) \sigma_{dip}(x, \mathbf{r}^2)$$

$$\begin{aligned} \Phi_T(z, \mathbf{r}, Q^2) &\equiv \Psi_T^*(z, \mathbf{r}, Q_1^2 = Q^2) \Psi_T(z, \mathbf{r}, Q_2^2 = 0) \\ &= \frac{6\alpha_{em}}{4\pi^2} \sum_f e_f^2 \left\{ [z^2 + (1-z)^2] \varepsilon_1 K_1(\varepsilon_1 r) \varepsilon_2 K_1(\varepsilon_2 r) \right. \\ &\quad \left. + m_f^2 K_0(\varepsilon_1 r) K_0(\varepsilon_2 r) \right\} \end{aligned}$$

$$\varepsilon_{1,2}^2 = z(1-z) Q_{1,2}^2 + m_f^2; \quad Q_1^2 = Q^2 \text{ and } Q_2^2 = 0$$

- The saturation models are input for  $\sigma_{dip}(x, \mathbf{r}^2)$ .

# The Saturation Model

- Golec-Biernat, Wusthoff: *Phys. Rev. D* 59 (1999) 014017.
- Model provides color transparency behavior at small  $r$  and constant dipole cross section at large  $r$ , with transition given by the saturation scale  $Q_{\text{sat}}(x)$ .

$$\sigma_{\text{dip}}(\tilde{x}, r^2) = \sigma_0 \left[ 1 - \exp\left(-\frac{Q_{\text{sat}}^2(x) r^2}{4}\right) \right]$$

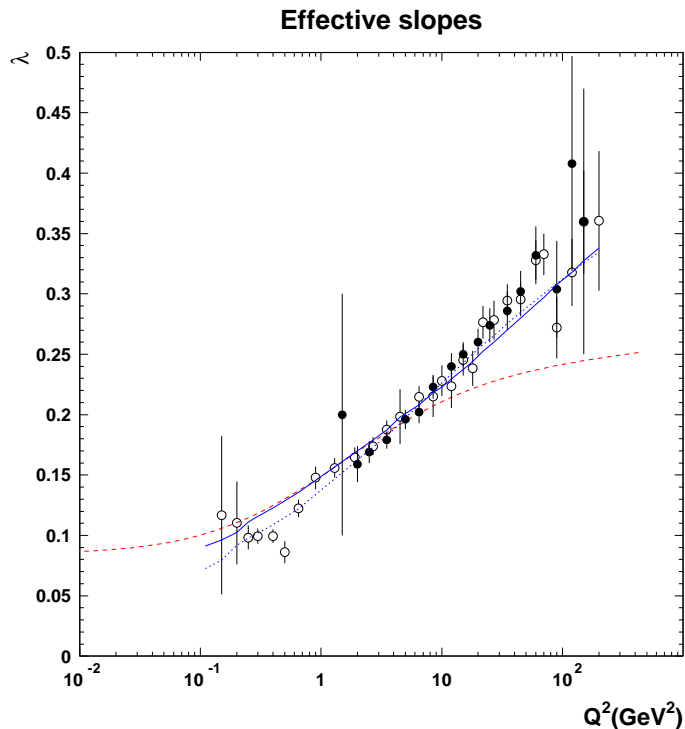
$$Q_{\text{sat}}^2(x) = \left(\frac{x_0}{\tilde{x}}\right)^\lambda \text{ GeV}^2; \quad \tilde{x} = x_{Bj} \left(1 + \frac{4m_f^2}{Q^2}\right)$$

- Parameters fitted from small  $x \leq 10^{-2}$  DESY-HERA data.
- 3-flavor (4-flavor) fit to  $\sigma_{\text{tot}}^{\gamma^*p}$ :  $\lambda = 0.288$  (0.277),  
 $x_0 = 3 \times 10^{-4}$  ( $0.34 \times 10^{-4}$ ),  $\sigma_0 = 23$  (29) mb.

# Entering DGLAP evolution . . .

- Bartels, Golec-Biernat, Kowalski: Phys. Rev. D 66 (2002).
- Improvement at high  $Q^2$  through DGLAP evolution.

$$\sigma_{dip}(\tilde{x}, r^2) = \sigma_0 \left[ 1 - \exp \left( - \frac{\pi^2 r^2 \alpha_s(\mu^2) \tilde{x} G(\tilde{x}, \mu^2)}{3 \sigma_0} \right) \right]$$

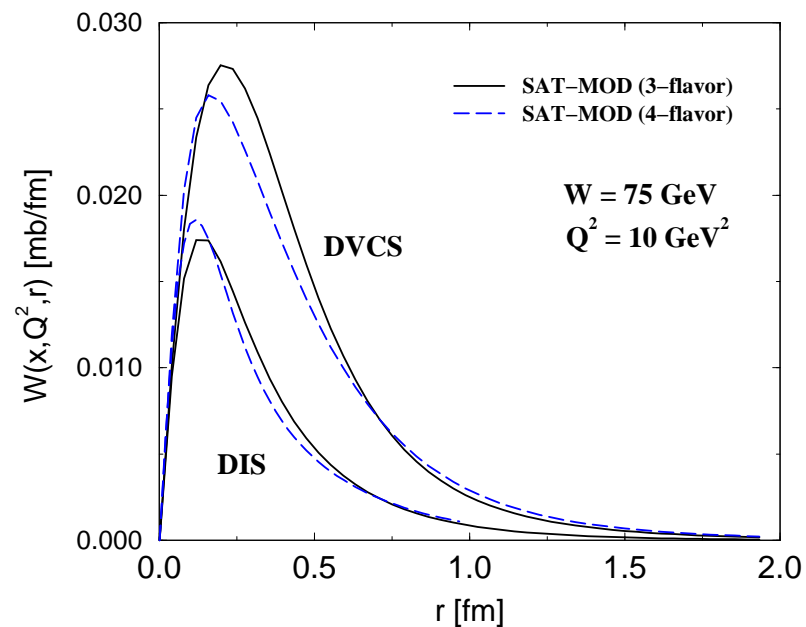
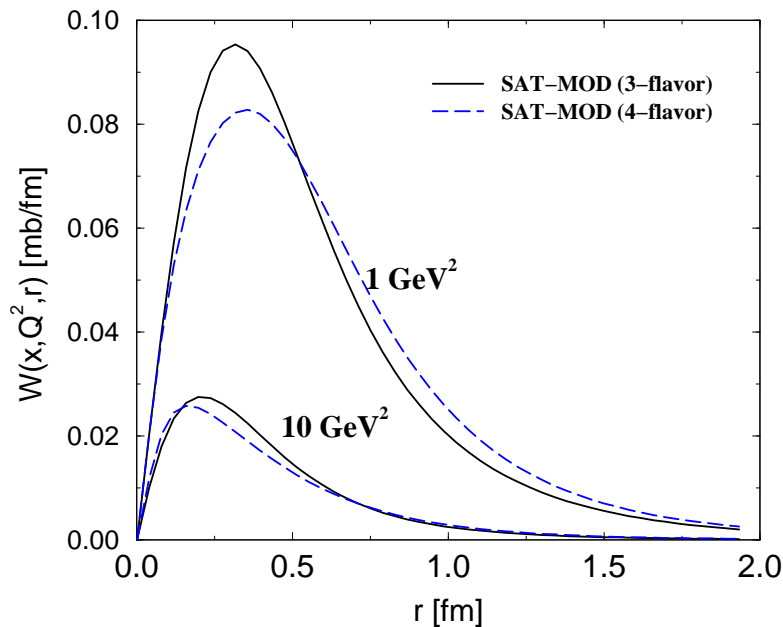


$$x G(x, Q_0^2) = A_g x^{-\lambda_g} (1-x)^{5.6}$$

$$\mu^2 = \frac{C}{r^2} + \mu_0^2$$

# Qualitative results . . .

- DVCS contains important contributions from  $r^2 \leq 1/Q_{\text{sat}}^2(x)$  in contrast to DIS.



- Saturation model offers a qualitative picture for DVCS.

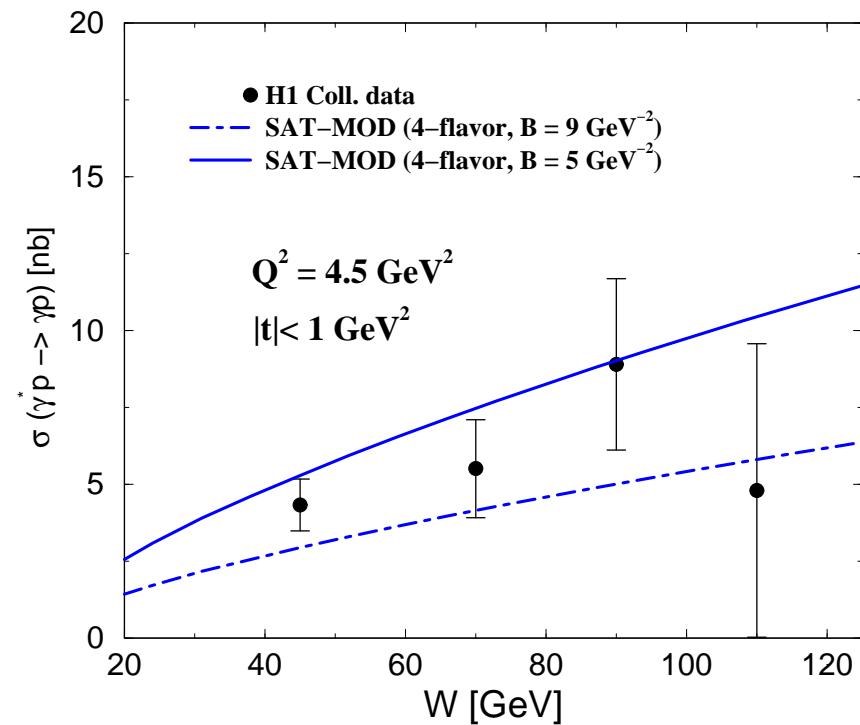
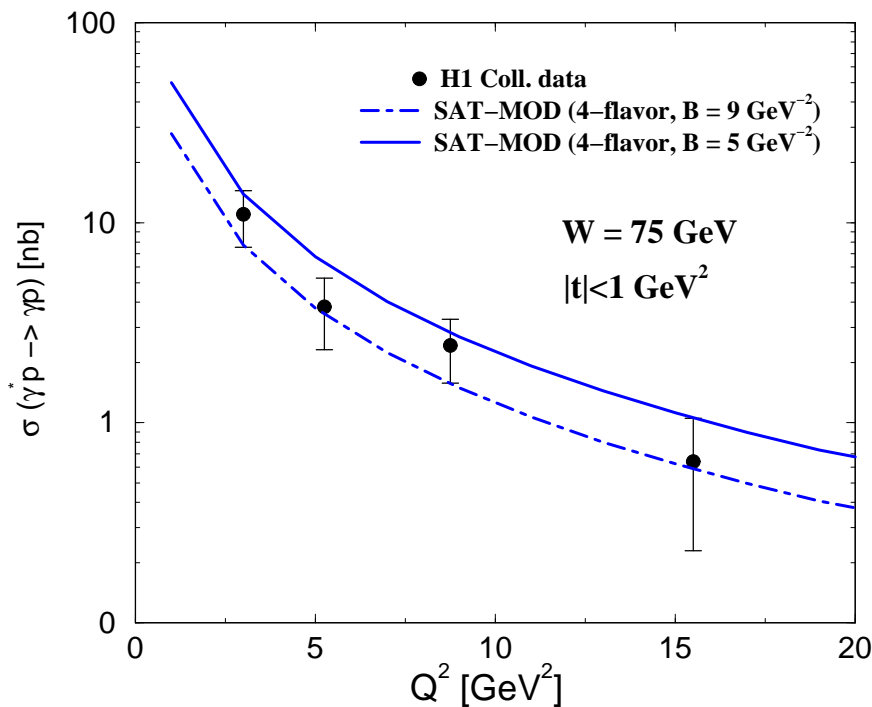
$$\text{Large } Q^2 : \sigma_{\text{tot}} \propto \frac{W^{4\lambda}}{Q^4}$$

$$\text{Small } Q^2 : \sigma_{\text{tot}} \propto \mathcal{C} \log^2(W^2)$$

# Results versus DVCS data at HERA

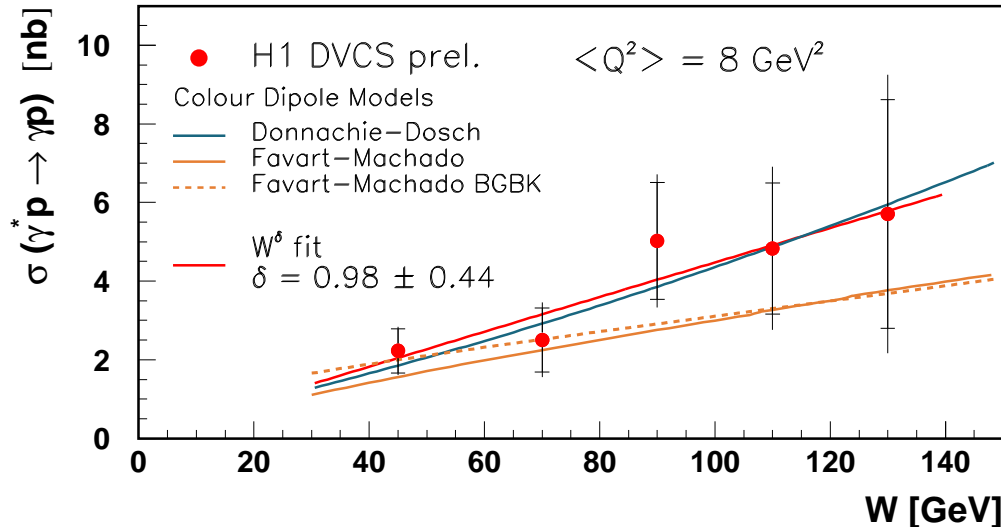
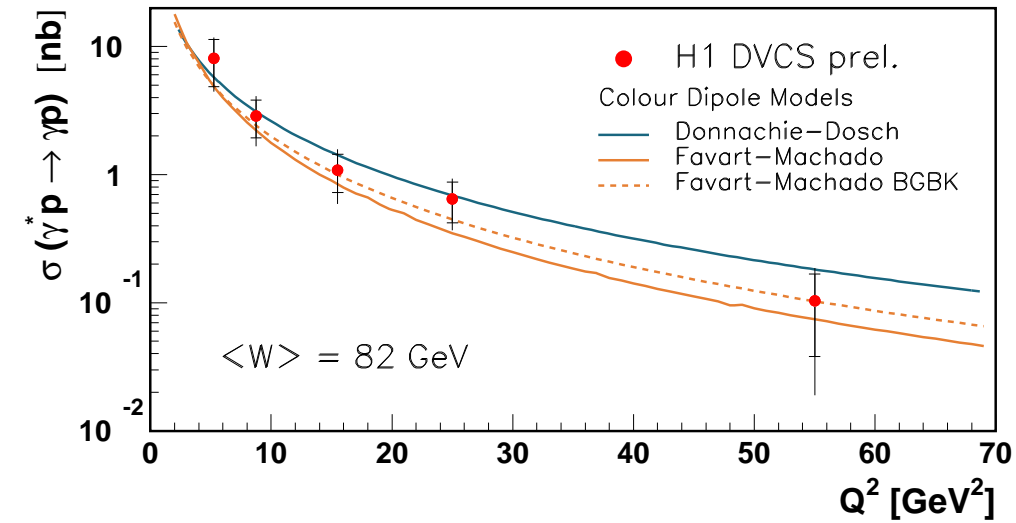
- DVCS cross section is obtained in a parameter free way.

$$\sigma(\gamma^* p \rightarrow \gamma p) = \frac{[\text{Im } \mathcal{A}(s, 0)]^2}{16 \pi} (1 + \rho^2); \quad \rho : \text{real by imaginary part}$$



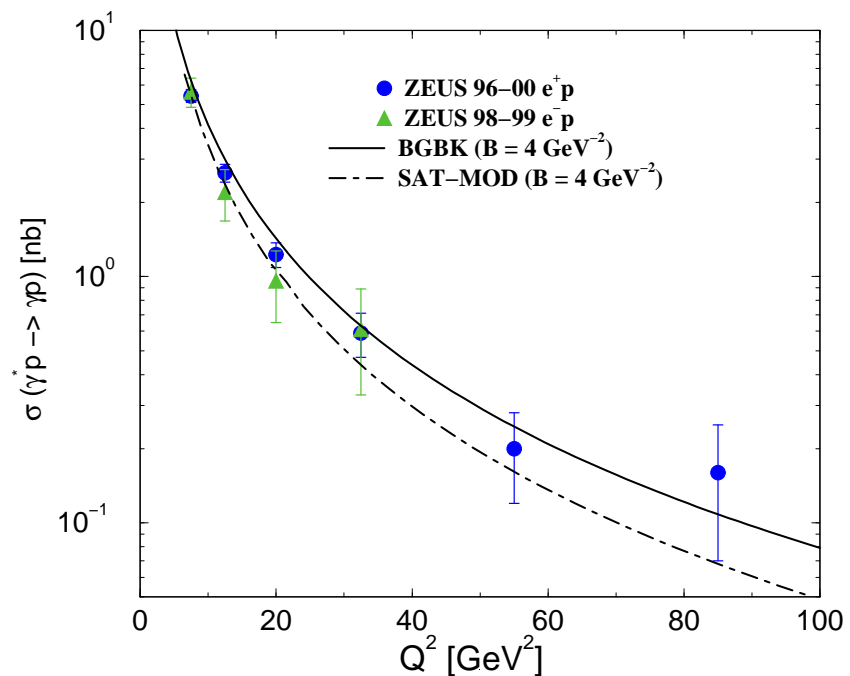
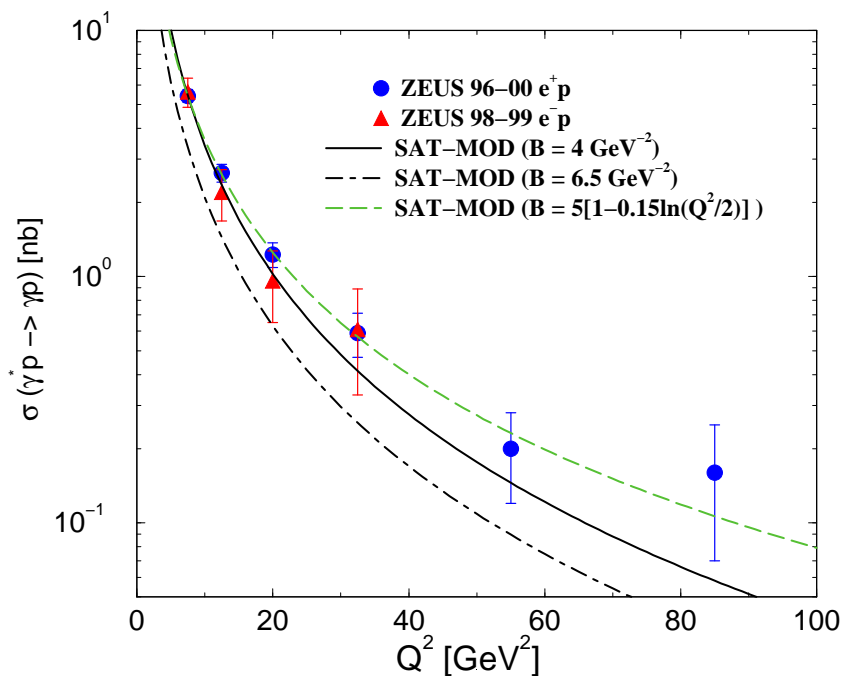
# Results versus new H1 DVCS data

● hep-ex/0312013 (proceedings of EPS HEP2003).



# QCD evolution at high $Q^2$

- Saturation model underestimates large  $Q^2$  ZEUS data.
- Investigating DGLAP QCD evolution (BGBK).



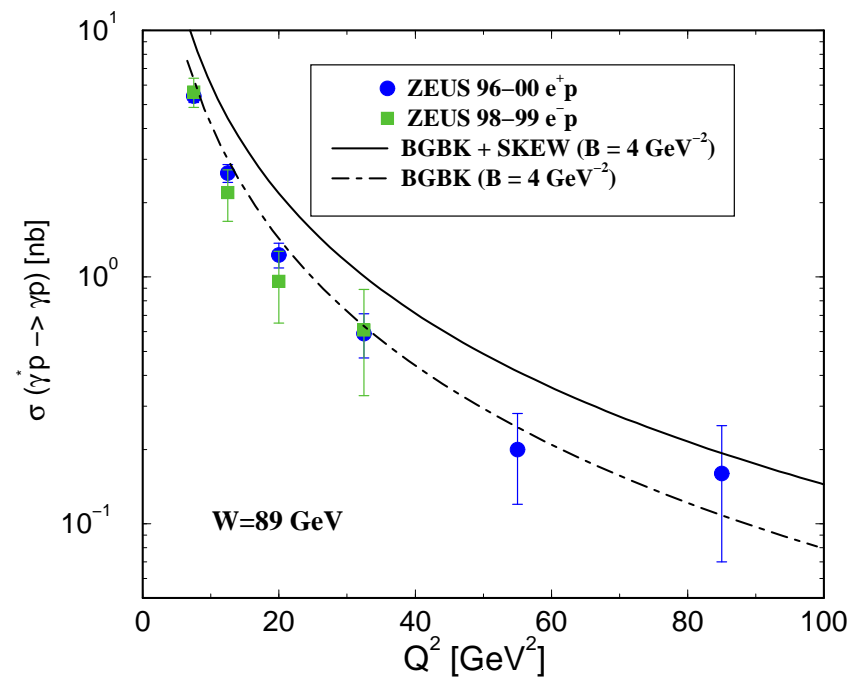
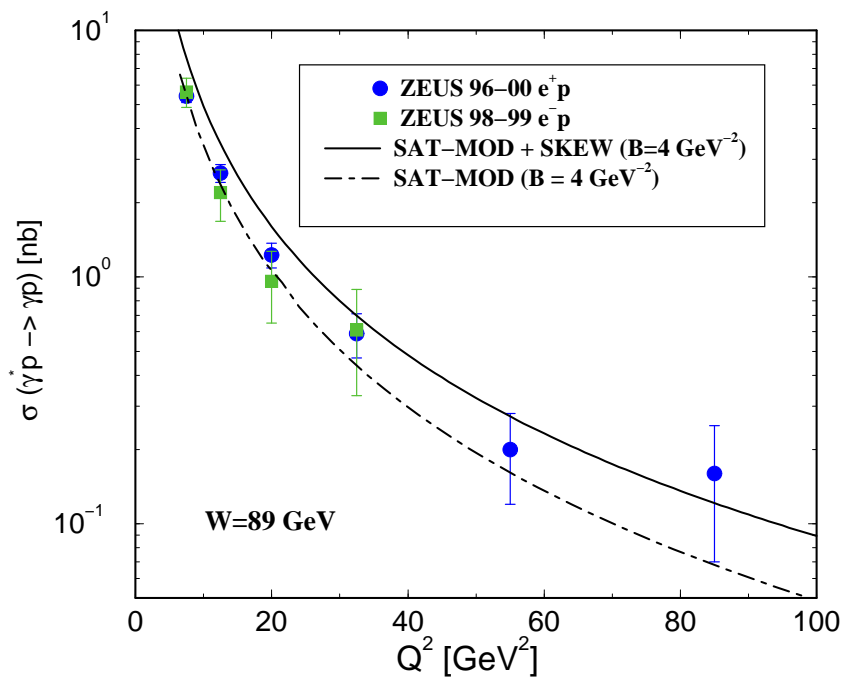
- Favart-Machado, [hep-ph/0402018](#) (EPJC)
- Skewedness effects are increasingly important at  $Q^2$ .

# Off-forward (skewed) correction

- Ratio of off-forward to forward pdf's [Shuvaev et al., Phys. Rev D60 014015 (1999)]

$$R_g(Q^2) = \frac{2^{2\lambda+3}}{\sqrt{\pi}} \frac{\Gamma(\lambda + \frac{5}{2})}{\Gamma(\lambda + 4)},$$

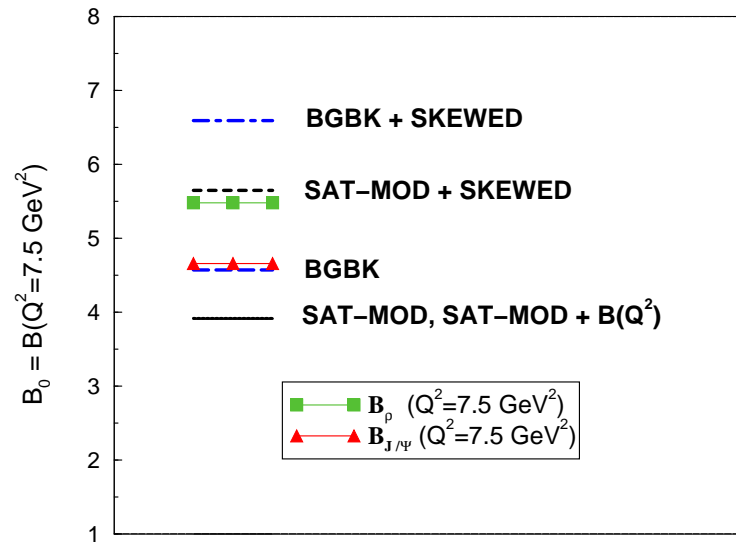
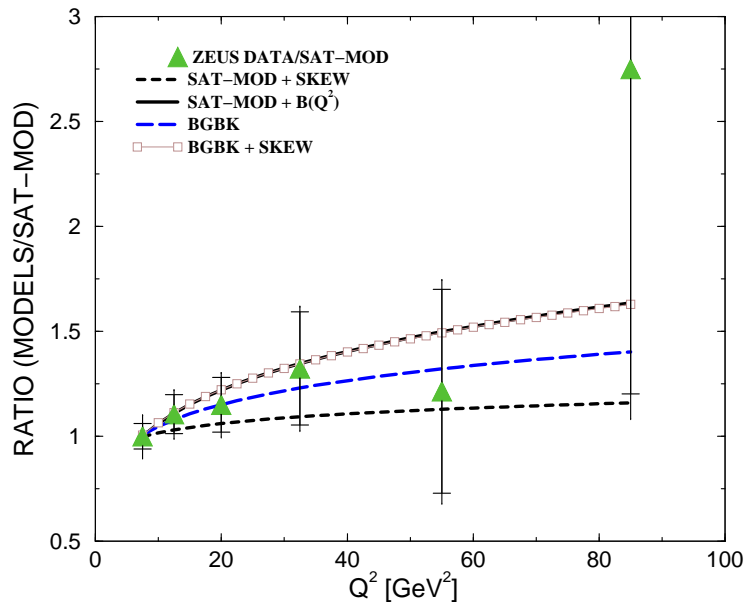
$$\lambda = \frac{\partial \text{Im} \mathcal{A}_{\text{DVCS}}}{\partial \ln(1/x)}$$



- Sizable contribution, mostly at large  $Q^2$ .

# Investigating both effects . . .

- Hard to disentangle models: slope parameter  $B$  has never been measured for DVCS.
- Analysing separately effects on  $Q^2$  dependence and overall normalization.



- Combination of effects can not be distinguished with the present experimental precision

# Summary

- DVCS process is an important tool to study QCD predictions and test phenomenological models.
- Dipole models, in particular those including saturation, describe in a parameter free way DVCS data.
- Saturation models and its extension to higher  $Q^2$  do excellent job in describing H1 and ZEUS measurements.
- Needed of an accurate slope measurement in a wide range of  $Q^2$ .
- Large  $Q^2$  data required to see QCD evolution/skewedness corrections.
- Hard to disentangle models/effects within current data precision.